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A Buddy for Betelgeuse: Binarity as the Origin of the Long Secondary Period in α Orionis

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Abstract

We predict the existence of α Ori B, a low-mass companion orbiting Betelgeuse. This is motivated by the presence of a 2170 day long secondary period (LSP) in Betelgeuse's lightcurve, a periodicity that is \approx 5 times longer than the star's 416 day fundamental radial pulsation mode. While binarity is currently the leading hypothesis for LSPs in general, the LSP and the radial velocity (RV) variations observed in Betelgeuse, taken together, necessitate a revision of the prevailing physical picture. Specifically, the lightcurve–RV phase difference requires a companion to be behind Betelgeuse at the LSP luminosity minimum, \approx 180° out of phase with the system orientation associated with occultation. We demonstrate the consistency of this model with available observational constraints and identify tensions in all other proposed LSP hypotheses. Within this framework, we calculate a mass for α Ori B of $M \sin i = 1.17 \pm 0.7 M_{\odot}$ and an orbital separation of 1850 \pm 70 R_{\odot} , or $2.43^{+0.21}_{-0.32}$ times the radius of Betelgeuse. We then describe the features of the companion as constrained by the fundamental parameters of Betelgeuse and its orbital system, and discuss what would be required to confirm the companion's existence observationally.

Unified Astronomy Thesaurus concepts: Long period variable stars (935); Binary stars (154); Red supergiant stars (1375); Circumstellar dust (236); Massive stars (732); Stellar pulsations (1625); Pulsation modes (1309)

1. Introduction

Interest in Betelgeuse, more formally known as α Orionis, has blossomed over the past five years due in large part to its anomalously severe dimming observed between the end of 2019 and beginning of 2020 (E. F. Guinan et al. 2019; A. K. Dupree et al. 2020; G. M. Harper et al. 2020). Now widely understood to have been caused by a dust cloud (M. Montarges et al. 2021), the "Great Dimming" nonetheless inspired many groundbreaking investigations into our nearest supergiant. These studies have led to revisions in our understanding of Betelgeuse's behavior and fundamental parameters, as well as opened new lines of inquiry into some of Betelgeuse's less well-understood properties, such as its apparent 5 km s⁻¹ surface rotation rate (J.-Z. Ma et al. 2024), the characterization of its variability (D. Jadlovský et al. 2024), and the classification of its pulsation modes (M. Jovce et al. 2020; M. MacLeod et al. 2023; H. Saio et al. 2023).

A distinctive variability cycle observed in Betelgeuse is an ≈2100 day period in the lightcurve (LC; see, e.g., L. L. Kiss et al. 2006; M. Joyce et al. 2020; T. Granzer et al. 2022; M. MacLeod et al. 2023), often labeled a long secondary period (LSP). LSPs are seen in many cool, luminous stars ranging from red giant branch (RGB) stars (e.g., P. R. Wood et al. 1999), asymptotic giant branch (AGB) stars (e.g., A. A. Zijlstra & T. R. Bedding 2002; S. Uttenthaler et al. 2015), post-AGB stars (H. Van Winckel et al. 1999; A. Bódi et al. 2016), yellow hypergiants (e.g., J. R. Percy & R. Y. H. Kim 2014), and red supergiant (RSG; e.g., L. L. Kiss et al. 2006) stars, in all cases

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showing generally steady periods ranging from hundreds to thousands of days (e.g., M. Takayama 2023). LSPs are an as yet unexplained class of stellar variability, called "secondary" because LSPs are typically a few to ten times slower than their host stars' radial fundamental pulsation modes (FMs).

Outstanding among the questions raised by renewed fascination with and deeper investigation into Betelgeuse is whether Betelgeuse's prominent, ≈2100 day periodicity is an LSP or the FM. The answer to this question carries significant implications for Betelgeuse's current evolutionary phase, which in turn implies the timeline for Betelgeuse's death in a supernova explosion (J. C. Wheeler et al. 2017; S. Nance et al. 2018; E. Chatzopoulos et al. 2020; H. Saio et al. 2023). If the ≈2100 day periodicity is the FM, it implies a large and observationally contentious radius for Betelgeuse. Further, it would place Betelgeuse's current evolutionary stage beyond the onset of core carbon burning, suggesting that a supernova explosion is imminent within the next several dozen to several hundred years (H. Saio et al. 2023). If, on the other hand, the 2100 day periodicity is an LSP, Betelgeuse is comfortably within in its core helium-burning phase and not due for an explosion for hundreds of thousands of years (M. Joyce et al. 2020). As we discuss below, most studies directly or indirectly support classifying the \approx 420 day periodicity as the FM. As such, the cause of Betelgeuse's 2100 day periodicity remains elusive.

There have been several mechanisms proposed to explain LSPs in general, ranging from giant cell convection, mode interactions, nonradial pulsations, and binarity, as well as more exotic physics, such as dust modulation beyond the stellar surface (many of these are discussed in P. R. Wood et al. 2004a). We explore the relative merits of each of these and more hypotheses proposed in the literature individually in the

context of modern observational data (see Section 4). We ultimately identify binarity as the most likely among them.

The idea that binarity could explain LSPs dates back to the late 1990s and early 2000s (P. R. Wood et al. 1999, 2004b) and has been reinforced since by the sequences formed by variable stars on period-luminosity diagrams (I. Soszyński 2007) and in radial velocity (RV) data (K. H. Hinkle et al. 2002; C. P. Nicholls et al. 2009). While such early versions of the binarity hypothesis were most concerned with whether a close companion could induce low-frequency modes on the primary star, the current leading theory is that the timescale of the LSP period is set by the orbital time of a low-mass companion, and the mechanism of dimming and brightening involves the formation and removal of dust along the line of sight in phase with the companion's orbit (I. Soszyński et al. 2021). Additionally, it has been proposed before that Betelgeuse is a multiple system (M. Karovska et al. 1986) from speckleimaging measurements, inferred to be two high-eccentricity companions including one at a separation of 0.00 with a period of 2.1 yr, which has not been confirmed in follow-up work with higher-resolution instruments (e.g., R. W. Wilson et al. 1992; P. Kervella et al. 2009; M. Montargès et al. 2016).

In this paper, we explore the implications and requirements of the binarity-as-LSP model for α Ori. In Section 2, we discuss LSPs in cool, evolved stars in the context of the periodluminosity sequences formed by classical variable stars and consider where Betelgeuse fits into this picture. In Section 3, we compare the brightness and RV variations observed in Betelgeuse and a significant subset of Gaia LSP stars and discuss the physical implications of the LC-RV phase offsets. In Section 4, we overview all of the scenarios proposed as an explanation for Betelgeuse's LSP, demonstrating critical flaws in all but one case: Betelgeuse has a companion that interacts with the star's dusty circumstellar environment. In Section 5, we derive the properties this companion must have based on observational constraints (Section 5.1) and discuss the conditions under which it should be observable (Section 5.2). We summarize and present our conclusions in Section 6.

2. Long Secondary Periods in Cool Evolved Stars

LSPs, sometimes referred to as P_2 in older literature, are a common but not ubiquitous phenomenon in cool evolved stars. They have been observed in $\approx 30\%$ of long-period variables (LPVs; see, e.g., I. Soszyński et al. 2021; M. Pawlak et al. 2024) and have been detected both in the Milky Way and in the Magellanic Clouds (see, e.g., C. Payne-Gaposchkin 1954; P. R. Wood et al. 1999; L. L. Kiss et al. 2006; I. Soszyński et al. 2009, 2011, 2013). These stars have large, radially extended convective envelopes, and with increasing luminosity, the convection in their envelopes can become near- or transsonic, with large-scale convective plumes spanning large fractions of the stellar radius (see, e.g., the review by A. Chiavassa et al. 2024). Stars hosting LSPs by definition show other pulsation modes, which are identified as low-order radial pressure modes (e.g., FM and first overtone (O1)).

Large sky surveys targeting the Magellanic Clouds, such as the MACHO and Optical Gravitational Lensing Experiment (OGLE) surveys (C. Alcock et al. 1997; A. Udalski et al. 1992; A. Udalski 2003), revealed that variability in red giant stars fall onto multiple, nearly parallel period–luminosity (*P–L*) relations, which were originally labeled from A to D (P. R. Wood et al. 1999). Sequences A, B, and C were attributed to pulsation

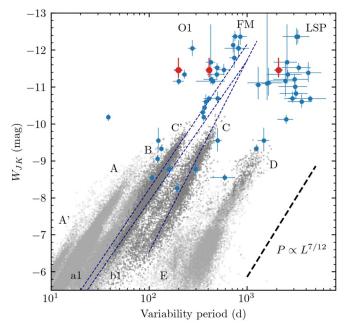


Figure 1. Period–Wesenheit (*P–W*) luminosity relations for the OGLE-III LPVs in the LMC (gray), and for Galactic RSGs (blue) collected by L. L. Kiss et al. (2006) based on absolute *J-* and *K-*band magnitudes. Red points, from left to right, mark the positions of the O1, FM, and LSP periodicities for Betelgeuse. Darker gray points are semiregular and Mira variables pulsating in the FM and O1 modes. Thin dashed lines indicate various *P–W* relations for RGB, AGB, and Mira stars in the LMC from I. Soszyński et al. (2007).

modes, whereas a fifth sequence, E, was attributed to eclipsing binaries (A. Derekas et al. 2006). Sequence D included the LSPs, which were found to be too long to be radial pulsation modes. We reproduce the sequences for the LMC from the OGLE-III survey in Figure 1, which includes the later identified A' and C' sequences (I. Soszyński et al. 2009). Here we plot the absolute K magnitudes of the stars, after crossmatching the OGLE catalog with the IRSF Magellanic Clouds Point Source Catalog (D. Kato et al. 2007) using a distance modulus of $\mu_{\rm LMC} = 18.54$ mag (P. Wielgórski et al. 2022).

Classical pulsating stars have been known to form P-L relations thanks to the pioneering work of H. S. Leavitt & E. C. Pickering (1912). These extend from classical Cepheids to other classes, such as Type II Cepheids, RR Lyrae, and δ Scuti stars, but also to red giants, semiregular stars, and Mira stars (Wyrzykowski et al. 2012). Many authors, e.g., J. Yu et al. (2020) and M. Trabucchi et al. (2017), have studied how the red giant sequences relate to specific modes. The latter work concluded that sequences A', A, and B correspond to the third, second, and first radial overtones, respectively, while C' and C separate less clearly due to the combined presence of RGB and AGB stars. C' includes both overtone and FM stars, whereas C is largely composed of Mira stars, which are AGB stars pulsating in the FM (e.g., L. Molnár et al. 2019; M. Joyce et al. 2024).

LSPs in sequence D also follow a period-luminosity relationship that is distinct from the *P-L* relations discussed so far. Sequence D was discovered by P. R. Wood et al. (1999) using MACHO data. Binarity was proposed as a possible mechanism for the LSP by various authors (K. H. Hinkle et al. 2002; E. A. Olivier & P. R. Wood 2003; P. R. Wood et al. 2004b). This was reaffirmed when A. Derekas et al. (2006)

showed that sequence D is an extension of sequence E (eclipsing binaries).

These sequences can also be extended further into the RSG regime (also shown in Figure 1). L. L. Kiss et al. (2006) found that Galactic supergiants form sequences that correspond to the O1, FM, and LSP periodicities and extend from sequences B, C, and D, respectively. We recalculated the M_I and M_K absolute brightnesses of this RSG sample, using Gaia Data Release 3 (DR3) distances from the catalog of C. A. L. Bailer--Jones et al. (2021) and plot these as blue filled circles in Figure 1. These distances were sufficient in most cases, but a few very bright stars required other sources for parallax (F. van Leeuwen 2007; M. J. Reid et al. 2019). For Betelgeuse, we used the distance calculated by M. Joyce et al. (2020), shown as red filled circles. Here we show W_{JK} Wesenheit indices as a proxy for luminosity based on the (J-K) colors, using the equation $W_{JK} = K - 0.686(J - K)$, because that limits the effects of interstellar reddening and helps to separate the sequences better (T. Lebzelter et al. 2019).

Compared to the original plot by L. L. Kiss et al. (2006), the O1 and FM sequences reproduced in Figure 1 appear to be considerably tighter. However, mode assignment based on P-L or P-W relations can be complicated as the constituent stars may belong to very different evolutionary stages, luminosity regimes, and variability classes that follow different relations. To illustrate this, we include three different P-W relations with blue dashed lines, computed by I. Soszyński et al. (2007), who identified further sequences and substructures in the red giant sample. The P-W relation running through sequence C belongs to the Mira stars, whereas a1 and b1 belong to the lower-luminosity AGB and RGB stars, respectively. The FM supergiants lie close to the extrapolations of these relations. We discuss modal assignment in more detail and based on further arguments in Section 4.1.

The RSG LSP periods in Figure 1 show larger scatter and have larger uncertainties, but appear to form a coherent extension of sequence D. The periods identified in Betelgeuse as O1, FM, and LSP align with the RSG sequences. In the case of radial pressure modes, in which the pulsation period is determined by the stellar radius and the average sound speed, a *P*–*L* relation is expected, as the period scales with average density, thereby radius and mass, and thereby luminosity. In this case, the longest possible radial pressure mode is the FM. The apparent existence of a *P*–*L* relation in the LSP, on the other hand, is puzzling prima facie. Gravity modes can yield periods below the FM, but no such period–luminosity relation exists for *g*-modes.

Unless the LSP phenomenon is simply a ubiquitous off-by-one error in the classification of the FM (see Section 4.1), LSPs appear impossible to explain with conventional pulsation theory when considering only material within the stellar photosphere as the "star." Whether the LSP is a pulsation or something else entirely, its period must be set by something other than the acoustic timescale of the star itself. As such, the LSP must operate on timescales longer than the dynamical timescale at the stellar surface $t_{\rm dyn} = R/v_{\rm esc}$, which is equivalent to the timescale of a Keplerian orbit at a distance equal to the stellar radius.

It is reasonable to ask why something without an intrinsic source of variability would nonetheless display a *P–L* relation. For this we can look outside the surface of the star, and make a dynamical argument. Generically, for a virial fluid element or

body outside the stellar radius, a period is set by the Keplerian orbital timescale at that location. Although a generic orbit is not sensitive to the stellar luminosity, any orbital architecture knows about the stellar mass and radius, as a > R, where a is the distance from the center of the star to the external location setting the LSP timescale, i.e., the orbital separation.

If a scales with R, then we can estimate

$$P = 2\pi \sqrt{\frac{a^3}{GM}} \propto \frac{R^{3/2}}{M^{1/2}} \propto L^{7/12},\tag{1}$$

where the last proportionality makes use of the approximations that (1) $L \propto M^3$ for gas-pressure-dominated stars and (2) $L \propto R^2 T_{\rm eff}^4 \propto R^2$. This is appropriate since the surface temperature ranges for RSGs, RGBs, and AGBs do not vary substantially relative to L. Notably, the zero-point of this relation would depend on the exact relationship between a and R, which introduces scatter in the scaling relation. This crude scaling argument nonetheless illustrates that any period sensitive to a star's radius and mass, such as one set by dynamics outside the stellar surface, is in turn sensitive to the star's luminosity.

A notable feature of observed LSPs is that they appear more prominently in bluer bands, though the effective temperatures of their host stars are not thought to change dramatically (M. Takayama et al. 2015; Gaia Collaboration et al. 2023a). This suggests that LSPs are likely related to the formation, destruction, modulation, or attenuation of dust around stars. However, dust alone cannot explain the LSP phenomenon; the presence of a dust-modulating mechanism is also required. When searching in visual passbands, I. Soszyński et al. (2021) found that only the attenuation by the cloud was visible. However, they identified secondary eclipses at longer wavelengths from Wide-field Infrared Survey Explorer (WISE) photometry, which is capable of detecting IR radiation from the dust cloud directly. I. Soszyński et al. (2021) thus conclude that LSPs arise when a small companion orbits the star together with an extended dust cloud.

Despite what we know about LSPs observationally and what we can infer about them theoretically, they remain to date the only form of steady-state stellar variability without a strong consensus on the underlying physics.

3. Characterizing the Lightcurve–Radial Velocity Phase Offset

An important diagnostic for the nature of pulsational versus orbital behavior is the presence or lack of RV modulations and the phase relative to brightness fluctuations.

Figure 2 shows the recent LC and RV variations for Betelgeuse side by side. The photometric data include *V*-band observations collected by the American Association of Variable Star Observers (AAVSO) as well as the processed and rectified photometry of the star from the SMEI instrument (B. V. Jackson et al. 2004; P. Hick et al. 2007), originally published by M. Joyce et al. (2020). RV observations were collected for more than a decade with the STELLA robotic telescope at Tenerife (T. Granzer et al. 2022). From the latter, an LSP period of 2169 ± 5.3 days and a peak-to-peak amplitude of 5.36 ± 0.056 km s⁻¹ were determined.

We fitted both variations with the $P_{LSP} = 2170$ day periodicity, from which we calculate the phase offset

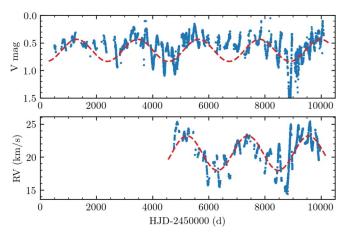


Figure 2. We show the photometric (*V*-band and SMEI from M. Joyce et al. 2020; and from the AAVSO) and RV (T. Granzer et al. 2022) variations for the star, plus single sine fits with red dashed lines, using the same 2170 day periodicity. Importantly, dimming in Betelgeuse's LSP always happens when the photosphere begins to move away from the observer, as indicated by the RV.

(T. Granzer et al. 2022; D. Jadlovský et al. 2023). This period value is consistent with other observations (L. L. Kiss et al. 2006; M. Joyce et al. 2020).

To determine the phase offset between the LC and RV for Betelgeuse, we follow the phase lag method described by R. Szabó et al. (2007), where we calculate $\Delta\phi_1=\phi_1^{\ \ RV}-\phi_1^{\ \ phot}$ from the phases of the fundamental component of the following Fourier fit to the data

$$f(t) = a_0 + \sum_{k=1}^{n} A_k \sin(2\pi f_k t + \phi_k),$$
 (2)

where a_0 is either the average brightness or the average (also called γ) velocity, f_k is the common frequency between the two data sets, and A_k and ϕ_k are the Fourier amplitude and phase components, respectively. For simplicity, we limit the fit to k = 1. However, we calculate the phase offset in Betelgeuse not just for the LSP but for the FM and O1 modes as well, based on the V-band and SMEI curves from M. Joyce et al. (2020), plus newer V-band observations collected by the AAVSO, truncated to the interval of the RV observations. We list our results for Betelgeuse in Table 1. The LC and pulsation periods of Betelgeuse are known to vary, and they went through considerable changes after the Great Dimming again, with O1 becoming the dominant pulsation mode instead of the FM (A. K. Dupree et al. 2022; D. Jadlovský et al. 2024). With the incorporation of new observations, the average periods of both modes shifted slightly relative to the values found by M. Joyce et al. (2020): the O1 became longer, whereas the FM became shorter, matching the period found by L. L. Kiss et al. (2006).

Figure 3 shows the phase offsets between Betelgeuse's LC and RV curve in the context of similar stars measured with Gaia. We compare Betelgeuse to a limited sample of LPV-candidate Gaia stars from Gaia Collaboration et al. (2023a) for which we could estimate the phase offsets. The data presented here is compiled in the Appendix. We also show the pulsational phase lags for classical Cepheids for comparison, including high-precision data for 87 stars from the work of R. Szabó et al. (2007), and lower precision data from Gaia DR3 for about 800

Table 1Fitted Periods, Fourier Amplitudes, and Phase Differences for the *V*-band and Radial Velocity Observations of Betelgeuse We Use in This Paper

ID	P (day)	A_1^V (mag)	$A_1^{RV} $ (km s ⁻¹)	$\Delta_{\phi_{ ext{RV}-V}}$	$e\Delta\phi$
LSP	2170	0.084(4)	2.62(2)	-1.990	0.027
FM	380	0.088(4)	1.45(2)	-1.322	0.058
O1	216	0.075(4)	1.72(2)	-0.435	0.059

stars for which phase data are included in the database directly (V. Ripepi et al. 2023).

Under the adiabatic assumption, one would expect radial pulsation to have a $-\pi/2$ offset where maximum brightness corresponds to maximum compression, i.e., to zero pulsation velocity on the descent from RV maximum. In reality, the phase offset is closer to zero $(\Delta\phi\approx0)$ for pulsating stars, because ionization removes heat energy during the compression phase, thus introducing a phase lag (J. I. Castor 1968; R. Szabó et al. 2007). For Betelgeuse, we find a relatively large phase offset for the FM, although its amplitude dropped considerably after the Great Dimming, which makes the fit more uncertain. The phase offset for the O1 mode, which is currently dominating the light variations in Betelgeuse, agrees with that of the shorter-period pulsating stars.

To characterize the LSP beyond the specific context of Betelgeuse, we calculated the phase offsets for the LSP stars published by C. P. Nicholls et al. (2009), where OGLE-III *I*-band photometry was available. We also calculated phase offsets for a subset of stars that were proposed to be LSP candidates by Gaia Collaboration et al. (2023a), based on the recent Gaia Focused Product Release. Despite the fact that the Gaia data are generally sparse for these stars, we managed to process nearly a third (\approx 400 stars) of the full sample. The distributions of the two sets in Figure 3 agree well, with most stars saddling the $-\pi/2$ value. We also found a few targets with offsets close to $(-)\pi$.

Turning now to the binarity model of the LSP, the configuration proposed by I. Soszyński et al. (2021) postulates that minimum light would occur when the companion passes in front of the red giant, corresponding to the point at which the RV variation of the primary goes through zero on the descending branch. This would occur at $\Delta\phi \approx \pi/2$ or $-3\pi/2$ offset. However, as Figure 3 shows, we observe the opposite not only in Betelgeuse, but in the majority of the LSP stars.

4. Proposed Long Secondary Period Hypotheses

In light of the observations discussed above, we now review and reevaluate proposed hypotheses for LSPs, discussing the validity of each as it applies to Betelgeuse.

4.1. Hypothesis 1: The Long Secondary Period is Actually the Fundamental Mode

Recently, H. Saio et al. (2023) proposed that the \approx 2100 day periodicity observed in Betelgeuse is in fact Betelgeuse's FM rather than an LSP—a claim that is in tension with a number of other recent investigations (M. Joyce et al. 2020; A. K. Dupree et al. 2022; T. Granzer et al. 2022; R. Neuhäuser et al. 2022; M. MacLeod et al. 2023; L. Molnár et al. 2023; see also J. C. Wheeler & E. Chatzopoulos 2023 for a recent review). However, classifying the \approx 400 day periodicity as O1 and the

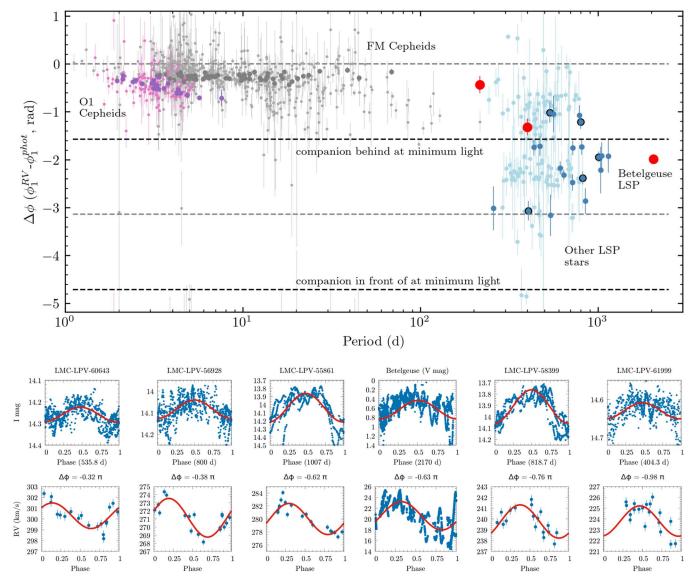


Figure 3. Upper: phase offset between the RV and photometric variations. Classical Cepheids from Gaia DR3 (Gaia Collaboration et al. 2023b; V. Ripepi et al. 2023) are shown with pink and light gray points, while stars from R. Szabó et al. (2007) are shown with purple and dark gray for FM and O1 stars, respectively, for reference. LSP stars from C. P. Nicholls et al. (2009) are shown with dark blue symbols, whereas Gaia DR3 LSP candidates from Gaia Collaboration et al. (2023a) are given in light blue. The O1, FM, and LSP points for Betelgeuse are shown in red (from left to right). Lower: OGLE *I*-band LCs and RV curves folded with the LSP periods, including sine fits for selected stars from C. P. Nicholls et al. (2009), ordered by decreasing phase offset, with Betelgeuse inserted into the sequence. Selected stars are marked with black outlines in the upper panel.

 \approx 2100 day periodicity as the FM cleanly resolves the question of the origin of the LSP in Betelgeuse by asserting that there simply is not one. This possibility is worth investigating.

M. Joyce et al. (2020) provided evidence that the 2100 day periodicity cannot be the FM on the basis that a periodicity of this length is not activated by the κ mechanism in either linear oscillation calculations performed with GYRE (R. H. D. Townsend & S. A. Teitler 2013; R. H. D. Townsend et al. 2018) or 1D hydrodynamic calculations performed with MESA (B. Paxton et al. 2011, 2013, 2015, 2018, 2019; A. S. Jermyn et al. 2023). Likewise, M. MacLeod et al. (2023) demonstrate that since the Great Dimming, Betelgeuse's FM oscillation was perturbed into a combination of overtones. As in M. Joyce et al. (2020), M. MacLeod et al. (2023) identify the \approx 400 day periodicity as the FM by performing adiabatic and nonadiabatic calculations with GYRE, exploring a larger range of spherical degrees than in M. Joyce et al. (2020; see their Table 1). Similarly, D. Jadlovský et al. (2024)

examine the behavior of shock waves in the aftermath of the dimming, coming to the same conclusion as M. MacLeod et al. (2023) that the dominant pulsation mode had transitioned from the FM to the O1.

In general, semiregular variable stars can exchange pulsational energy between p-modes, so an exchange between the FM and the O1 is possible, but an exchange between the FM and LSP is not. In particular, energy exchange between modes happens in semiregular stars for period ratios close to a 2:1 resonant ratio, which is the ratio of the \approx 400 day and \approx 200 day periods of Betelgeuse (J. R. Buchler et al. 2004). The fact that there was a mode switch from the \approx 400 day periodicity to a \approx 200 day periodicity observed right after the Great Dimming (also M. MacLeod et al. 2023), rather than a mode switch at the \approx 2100 day periodicity, is further evidence that the 400 days periodicity is the FM (as is the fact that 2100:400 is a \approx 5:1 rather than 2:1 ratio).

Another critical issue with the 2100 days as an FM hypothesis is the stellar radius required to sustain an acoustic mode with a period of $\approx\!\!2100$ days. As noted in H. Saio et al. (2023), a radius of roughly 1300 R_{\odot} is implied by models that treat Betelgeuse's 2100 day periodicity as the FM. Observational constraints on Betelgeuse's radius provided by X. Haubois et al. (2009), M. Montargès et al. (2014), and P. Kervella et al. (2018) are in tension with these calculations, even at the longest distance measurements, as discussed in detail in L. Molnár et al. (2023). Measurements that find angular diameters larger than 50 mas (corresponding to radii $>\!1100~R_{\odot}$) were done at longer wavelengths and thus sample the close molecular layers (i.e., the MOLsphere) above the photosphere (E. O'Gorman et al. 2017; E. Cannon et al. 2023).

Still other studies undermine the 2100 day FM hypothesis on strictly evolutionary grounds. For example, in an investigation focused on constraining Betelgeuse's present-day evolutionary stage, R. Neuhäuser et al. (2022) argue that Betelgeuse recently crossed the Hertzsprung gap, supported by its historically documented color change over the past several thousand years. A recent traversing of the Hertzsprung gap places Betelgeuse in the early stages of core helium-burning, which is incompatible with the core-carbon-burning evolutionary phase implied by a 2100 day FM (H. Saio et al. 2023).

Given the range of arguments against a 2100 day FM period from many orthogonal perspectives, we reject the claim that the pulsation mode widely classified as Betelgeuse's LSP is actually the star's FM. We proceed henceforth referring to the \approx 400 day periodicity as the FM and the \approx 2000 day periodicity as the LSP in Betelgeuse. While the case of Betelgeuse alone is enough to debunk the 2100 day FM hypothesis as a universal explanation for LSPs, the existence of sequence D on the $P\!-\!L$ diagram (see Figure 1) does so more conclusively.

4.2. Hypothesis 2: Giant Convective Cells

In light of the evidence that LSPs are not simply misidentified FMs, as discussed above, R. Stothers & K. C. Leung (1971) proposed the hypothesis that giant convective cells can explain the LSP phenomenon, generalized by R. B. Stothers (2010) to extend to all LSP pulsators. Broadly, while the acoustic FM timescale is limited by $\sim R/c_{\rm s}$ and thus predicts periods too short to explain the LSP for reasonable stellar radii and $T_{\rm eff}$, a hypothetical periodic signal might be mediated by the overturn timescale of giant convective cells

$$t_{\rm conv} = \ell/v_c, \tag{3}$$

where ℓ is the plume size and v_c is the characteristic velocity of convection. In the limit of low $v_c < c_s$ with a maximum plume size ℓ approaching R, this timescale can indeed be longer than the FM.

This picture has order-of-magnitude agreement in the luminosities and RV amplitudes (R. B. Stothers 2010). Following mixing length theory (MLT; E. Böhm-Vitense 1958; see the recent review by M. Joyce & J. Tayar 2023), the local characteristic length scale of convection can be expressed as $\ell = \alpha_{\rm MLT} H_P$ where H_P is the pressure scale height and $\alpha_{\rm MLT} \approx 2\text{--}4$ for RSGs (e.g., S.-H. Chun et al. 2018; J. A. Goldberg et al. 2022). In MLT, ν_c can then be estimated (R. Kippenhahn et al. 2013) from the superadiabaticity

 $\nabla - \nabla_{\rm e}$, the local gravity g, and thermodynamic properties

$$v_c^2 = gQ(\nabla - \nabla_e) \frac{\ell^2}{\nu H},\tag{4}$$

where ν is a geometric factor encoding plume geometry (typically $\nu = 8$ following L. Henyey et al. 1965 and others), $Q = -D \ln T/D \ln \rho$ is determined by the equation of state, and $\nabla - \nabla_{\rm e}$ can be related to the flux carried by convection ($F_{\rm conv}$) and the mixing length by

$$F_{\text{conv}} = \rho c_P T \sqrt{gQ} \frac{\ell^2}{\sqrt{\nu}} H^{-3/2} (\nabla - \nabla_{\!e})^{3/2},$$
 (5)

and where c_P is the specific heat at constant pressure.

In the extended convective envelopes of RGB stars, AGB stars, and RSGs, indeed $\ell \sim R$. In such a star, large $H_P/r \sim 0.25$ in the interior yields large-scale plumes spanning a sizeable fraction of the stellar radius, as recovered both by simulations (e.g., B. Freytag et al. 2002; S. B. F. Dorch 2004; A. S. Brun & A. Palacios 2009; B. Plez & A. Chiavassa 2013; A. Chiavassa et al. 2009, 2010a, 2010b, 2011, 2017, 2024; A. Antoni & E. Quataert 2022; J. A. Goldberg et al. 2022) and inferred from observations (e.g., M. Montargès et al. 2017; A. Chiavassa et al. 2018a, 2018b; K. Kravchenko et al. 2018, 2019, 2020, 2021; Z. Zhang et al. 2024). For RSGs like Betelgeuse, MLT predicts convective velocities of $\sim 5-25$ km s⁻¹ for RSG stars (see discussions in M. Joyce et al. 2020; J. A. Goldberg et al. 2022), somewhat consistent with the required convective velocity to give rise to an overturn time of period P in a star of radius R

$$v_{c,\text{LSP}} \equiv \frac{R}{P} = 2.8 \text{ km s}^{-1} \left(\frac{R}{764R_{\odot}}\right) \left(\frac{P}{2170 \text{ day}}\right)^{-1}.$$
 (6)

However, while there is order-of-magnitude agreement with the observed LSP, tensions arise. Large-scale convection is more or less ubiquitous in cool, luminous giants, and as such, we would expect all such stars to exhibit similar LSP behavior if giant convective cells were the cause. In reality, only 30% do (C. P. Nicholls et al. 2009; I. Soszyński et al. 2021). Moreover, convective motions do not remain coherent forever, even in the case of a giant convective cell, whereas LSPs are generally steady in nature. M. Takayama (2023), for example, found that of \approx 9000 LSP candidates in the LMC and SMC, only ≈150 of those candidates showed any evidence for a changing LSP duration over the observing term. In the convective picture, over time significant stochasticity is expected to be introduced into both the LCs and observed velocities, and eventually the stochastic variability should wipe out a periodic signal from convection alone. In fact, in the hotter OB star regime, variability from subsurface convection has been proposed to better explain stochastic low-frequency variability (W. C. Schultz et al. 2020; M. Cantiello et al. 2021), and in RSGs, similar stochastic variability from granulation has been recovered from LMC observations (e.g., Z. Zhang et al. 2024).

Giant convective cell models also make no prediction for RV modulation on the timescale of LSP. The convective velocity v_c is a characteristic velocity of convective transport and not simply a bulk fluid velocity, as plumes move upwards and downwards and laterally at the surface (R. F. Stein & A. Nordlund 1989; R. F. Stein & Å Nordlund 1998). In fact, the convective overturn time is often considered to be a decoherence time. In 3D simulations of RSG envelopes

J. A. Goldberg et al. (2022) found decoherence times on the order of $\approx 300-500$ days. Additionally, J.-Z. Ma et al. (2024) show that convective plumes in an RSG-like convective envelope could mimic a 5 km s⁻¹ signal inferred to be surface rotation (see, e.g., P. Kervella et al. 2018). However, they find that the coherence time and dipole orientation of such a signal are significantly less than their 5 yr of simulation time, with snapshots showing synthetic $v\sin i$ dipoles ranging from <1 to 10 km s^{-1} at random orientations.

The MLT treatment, which defines a single "convective velocity" scale and thus a single "convective overturn" timescale is, of course, a dramatic simplification of the true complexities of convection (see, e.g., M. Joyce & J. Tayar 2023, Section 5; as well as the discussion in Section 5 of J. A. Goldberg et al. 2022 in the case of RSGs, especially their Figure 19). Stars like Betelgeuse with large envelopes hosting vigorous convection are indeed more poorly approximated by MLT than solar-like stars by virtue of their significant deviation from solar conditions (see, e.g., M. Joyce & B. Chaboyer 2018). Locally, super-Eddington luminosities due to the presence of strong opacity peaks lead to numerical as well as physical challenges for 1D models, which must be overcome through various "engineering" techniques (see, e.g., Section 7.7 of B. Paxton et al. 2013; Section 7.2 of A. S. Jermyn et al. 2023, and discussions and references therein). Moreover, the convective motions observed in 3D radiation hydrodynamics simulations of near-surface convection in RSG envelopes and other luminous massive stars do not even resemble motions typical of MLT-like convection out to the surface (W. C. Schultz et al. 2020, 2022; J. A. Goldberg et al. 2022); above some radius (R_{corr}) the correlations between the radial fluid velocity and the density, entropy, and opacity invert—cold, dense, highopacity material which would sink in MLT-like convection is correlated with positive v_r —even at high optical depth $\tau \gtrsim 100.6$

At the very least, any modulated RV signal caused by giant convective cell turnover is likely to be far more complex than the RV modulation seen in Betelgeuse or the Gaia LSP variables, and an LSP driven by large-scale turbulent motions would not persist for the \gtrsim hundred years over which Betelgeuse has been observed.

4.3. Hypothesis 3: Mode Interactions (Beats)

Interaction between close-by modes can create long beating periods that could match the LSPs. However, beating modulates the pulsation amplitudes and hence the LC envelopes, but not the average brightness. Furthermore, if the LSP period were a beating period between modes in Betelgeuse, then it would correspond to a physical signal close to the pulsation frequencies. This signal would be offset by

about 19% and 10% relative to the FM or the O1 frequencies, instead being of an independent signal at $1/P_{\rm LSP}$.

Another aspect of mode interaction concerns interactions between the LSP and the other pulsation modes. If two (or more) strong pulsation modes are present in the star, they will both influence the envelope structure in which the other modes have to travel. These interactions would cause combination frequencies to appear in the frequency spectrum of the star, as seen in double-mode Cepheids and RR Lyrae stars (see, e.g., M. Gruberbauer et al. 2007). Such combination frequencies with the LSP would be very similar to the beating frequencies mentioned above (e.g., at $f_{\rm FM} \pm f_{\rm LSP}$). But such signals have not been reported for Betelgeuse, which suggests that the LSP is not the product of a beating phenomenon.

4.4. Hypothesis 4: Rotation

As noted in P. R. Wood et al. (2004a), if stars exhibiting LSPs are "rotating prolate spheroids," meaning they are distorted in such a way that the polar radius is larger than the equatorial radius, they would produce the velocity curves characteristic of LSPs. However, the rotational velocities that would be required for this explanation are far too high compared to observations: the apparent 5–15 km s⁻¹ surface velocity of Betelgeuse corresponds to a 30 yr periodicity, whereas Betelgeuse's LSP has a 5.5 yr periodicity. Further, LSPs fall on a period–luminosity sequence, and it is not clear why this would happen if (solid body) rotation were the explanation.

4.4.1. Differential Rotation

On the main sequence, the cores of high-mass stars have been predicted by some models to rotate about $100\times$ as fast as their surfaces (see, e.g., A. Heger et al. 2000, 2005), though more recent studies have shown that these models overpredicted core rotation by a factor of 10. In one such study, M. G. Pedersen (2022) found that measurements indicate that slowly pulsating B stars with masses of $5-10~M_{\odot}$ rotate close to rigidly. Conversely, J. J. Hermes et al. (2017) do find evidence of a connection between high stellar birth mass and rapid core rotation via asteroseismology of white dwarfs, although again for masses below that of Betelgeuse. There are currently no measurements of core rotation in stars above $10~M_{\odot}$, so extrapolation to Betelgeuse should be taken with caution.

Further, the relationship between envelope and core rotation along the main sequence is not necessarily preserved once the star enters the core helium-burning phase. B. Mosser et al. (2024) find that, for low-mass red giants, the evolution of the core rotation rate in core helium-burning stars scales with the inverse square of the stellar radius, in good agreement with J. Tayar et al. (2019). Although Betelgeuse is a massive star, and the core rotation rates of RSGs have not been probed directly, asteroseismic relations for low-mass, core heliumburning red giants are informative for this case. The model described in B. Mosser et al. (2024) is that of a rigid, dense helium core surrounded by a radiative layer with a smooth rotation profile, all encased by a rigid convective envelope; a picture that describes Betelgeuse reasonably well. Putting the M. Joyce et al. (2020) lower mass bound ($\sim 16.5~M_{\odot}$) and radius (764 R_{\odot}) for Betelgeuse into B. Mosser et al. (2024)'s Equation (3) yields a core rotation rate of approximately

While there are significant caveats with MLT in the context of defining a single persistent convective overturn time, it is unlikely that the simplifying assumptions of MLT discussed above would affect results in this work in any other way. As noted by M. Joyce et al. (2020), the primary impact of changing $\alpha_{\rm MLT}$ in models of 10– $25~M_{\odot}$ was to shift in temperature the location of the RGB, leading to a factor-of-ten increase in the uncertainty of the effective temperature constraint as compared to the error bars reported observationally by E. M. Levesque & P. Massey (2020). While uncertainty in the optimal value of the mixing length could certainly impact results through the impact of $\alpha_{\rm MLT}$ on the synthetic seismic frequency spectra against which Betelgeuse's pulsation spectrum was compared, this uncertainty was fully accounted for in M. Joyce et al. (2020), whose parameters we use elsewhere in our analysis.

400 days. This is much shorter than the LSP, so modulation by internal rotational is ruled out.

Though C. C. Lovekin et al. (2009) note that extreme cases of differential rotation will cause slight shifts in acoustic mode frequencies, the extent of such a shift would be nowhere near the factor of ≈ 5 decrease in frequency required to make the FM mimic the LSP. Further, A. S. Jermyn et al. (2020) find that there is very little radial differential rotation in stars with convective envelopes (in both short- and long-period eclipsing binaries) anyway.

4.5. Hypothesis 5: Magnetism

Various authors have explored the possibility that a process analogous to the magnetic solar cycle—e.g., star spots, convectively driven magnetic dynamo—could generate LSPs (e.g., N. Soker & G. C. Clayton 1999 in AGBs; P. R. Wood et al. 2004b in RSGs), but several problems arise with this theory (E. A. Olivier & P. R. Wood 2003). Of particular importance is the fact that spots on a rotating surface are not capable of explaining LC variations across the appropriate range of colors (i.e., the observed chromatic behavior, or chromaticity), as discussed in P. R. Wood et al. (2004b) and more recently in M. Takayama et al. (2015).

Another issue is that magnetic cycles in stars like Betelgeuse are expected to be much longer than 11 yr. Although there is no simple means of scaling the solar magnetic cycle to RSGs, and dynamo cycles have not been observationally confirmed in stars like Betelgeuse, we know that the period of the magnetic solar cycle goes as

$$T_{
m solar} \sim \frac{R^2}{n},$$
 (7)

where R is the stellar radius and η is the magnetic diffusivity. The magnetic diffusivity is a function of the scale of the convective motions in the envelope and the star's conductivity. Every term in this relation contributes to increasing the period of the magnetic cycle in Betelgeuse relative to that of the Sun. Given that the period of the LSP is roughly 5.5 yr (which is <11 yr), a magnetic cycle similar to the Sun's is not a viable explanation for the LSP in a large, evolved star with a deep convective envelope.

Some magnetic phenomena affecting high-mass stars are worth considering. The interplay between differential rotation and magnetic fields has been studied primarily in OB stars (A. Maeder & G. Meynet 2011, 2012), which was Betelgeuse's spectral type when it was on the main sequence. Z. Keszthelyi et al. (2019) find that fossil fields in massive stars can induce mass-loss quenching and magnetic braking; however, episodic mass loss is periodic and should happen at the frequency of the FM. The role of fossil fields would be to suppress the amount of mass dispersed per episode, not to alter the frequency of mass-loss episodes. Fossil fields therefore do not cause the LSP. Finally, while shorter-period, dynamo-generated magnetic fields can exist in the subsurface convection zones in hot, massive stars (M. Cantiello & J. Braithwaite 2011), Betelgeuse is not hot enough to have an iron opacity peak near the surface.

4.6. Hypothesis 6: Nonradial Pulsations

Any pulsation-related explanation for the LSP must involve a driving mechanism that produces pulsations below the frequency of the FM (see Section 4.1), which means it cannot be acoustically driven. Such drivers may be intrinsic or extrinsic to the star. Here we address the possibility that the LSP is caused by an intrinsic source of nonradial pulsations.

4.6.1. Strange Modes

Strange modes are unstable modes with potentially high growth rates that occur in extremely nonadiabatic environments dominated by radiative energy transport (H. Saio 2009). They are caused by a large difference in phase between the density and pressure maximum in the oscillating partial ionization zone. Strange modes can be found in the radial spectra of many luminous stars, including Cepheids, RR Lyrae, luminous blue variables, and other high-amplitude pulsators (J. R. Buchler et al. 1997). Their presence in luminous red giants is discussed in detail in P. R. Wood & E. A. Olivier (2014).

Strange modes with LSP-like periods have been found in red giant models, arising due to the interaction of stellar oscillations with convective energy transport (P. R. Wood 2000). However, such modes are highly damped, and models predict an exponential decay timescale of less than 100 days upon perturbation (P. R. Wood et al. 2004b). They are therefore highly unlikely to be observed in real stars.

More recently, H. Saio et al. (2015) argued that such oscillatory convective modes can, in fact, explain LSPs in real red giants. However, to generate modes of the correct period to reproduce sequence D (see Figure 1), H. Saio et al. (2015) engineered highly nonadiabatic stellar models dominated by radiative transport in their outermost layers, which do not accurately reflect the physics of RSGs. 3D simulations show that in fully convective RSG envelopes, the convective velocities penetrate above the surface. Large turbulent motions well outside the stellar photosphere form coherent plumes, meaning that while radiation carries much of the flux, the convective motions persist far above the photosphere (see, e.g., A. Chiavassa et al. 2009, 2011, 2024; J. A. Goldberg et al. 2022; J.-Z. Ma et al. 2024). In fact, at any radius defined as the "photosphere," there is even some fluid that is optically thick and retaining its entropy such that its behavior is convective even though radiation is carrying flux elsewhere along in the near-surface layers (see the discussion in Section 4.4 of J. A. Goldberg et al. 2022).

H. Saio et al. (2015) encoded the surface-radiation-dominated physics in their 1D models (computed with MESA) by using a low, very subsolar value for the convective efficiency ($\alpha_{\rm MLT}/\alpha_{\rm MLT,\odot}=1.2/1.8=0.67$) in the MLT formalism, and it is this choice that enables both the large surface radiative zones and large radii of their models. In reality, convection is more efficient in an RSG's envelope than it is in the Sun's (e.g., S.-H. Chun et al. 2018), with typical values of $\alpha_{\rm MLT}\approx 2-3$ inferred from observed H-R positions of nearby RSGs. Further, the use of $\alpha_{\rm MLT}=1.2$ produces models with inappropriately low effective temperatures (E. M. Levesque & P. Massey 2020).

Given the inability of models to reproduce simultaneously the correct RSG temperatures, convective envelope physics consistent with RSGs, LSP-appropriate strange mode frequencies, and strange mode lifetimes long enough to be observable, we reject strange modes as the explanation for the LSP of Betelgeuse.

4.6.2. g-modes

Because they can have longer periods than the radial FM, *g*-mode pulsations were first proposed as an explanation for the LSP by P. R. Wood et al. (1999). However, the structure of RSG envelopes once again undermines the viability of this explanation. As noted by M. Takayama et al. (2015) and discussed earlier in P. R. Wood et al. (2004b), *g*-modes must develop in a radiative zone. At best, LSP stars have a very thin outer radiative layer above their large convective envelopes. The size of this region strongly limits the amplitude of *g*-modes that could develop there, and any such modes would be too small to explain the large amplitudes of both the brightness and RV variations that characterize LSPs.

Inverting the argument, any g-mode that would be observationally detectable as the LSP in Betelgeuse implies the existence of a quiet, "well-behaved," and large-enough radiative zone near the surface of Betelgeuse in which this mode is propagating. Neither stellar evolution calculations nor models of large convective cells in RSGs suggest this is possible.

To comment briefly upon *g*-modes in the stellar core, we note that *g*-modes are evanescent (i.e., exhibiting amplitude decay over distance) throughout the convective envelope—which is, once again, enormous in Betelgeuse—and would therefore not be detectable at the stellar surface. We are thus left with the fact that *g*-modes can account for LSP periods but not LSP amplitudes, no matter their origin in RSGs.

4.7. Hypothesis 7: K mechanism in the Dust Shell

The final remaining pulsational scenario consistent with the LSP timescale posits a radial pulsation from a mechanism driven outside the optical stellar photosphere, dragging both the photosphere and the external material. J. M. Winters et al. (1994) and S. Hoefner et al. (1995) argue that opacity changes in the dust shell surrounding the star could cause oscillations via a "dust- κ " mechanism, whereby the strong temperature and density sensitivity of the sublimation state (and thus opacity) of circumstellar dust could induce radial pulsations in the dust shell(s) (see also the discussions by P. R. Wood et al. 2004b).

From a period–mean density relation with generic period Π

$$\Pi \propto \frac{1}{\sqrt{G\bar{\rho}}} \propto R^{3/2},$$
 (8)

where $\bar{\rho}$ is the average density and the second proportionality assumes the mass scale is dominated by the stellar material and not the dust. For an LSP:FM period ratio of \approx 5, assuming the FM is an oscillation at the (optical or IR) stellar photosphere, this would mean that the "outer" radius mediating the RV signal would be \approx 3 times the stellar radius, or \approx 2200 R_{\odot} for a radius of 764 R_{\odot} (M. Joyce et al. 2020). This is consistent with placement inside the region probed by radio observations indicating the presence of significant circumstellar dust from two to six stellar radii (W. J. Altenhoff et al. 1979; J. Lim et al. 1998; G. M. Harper et al. 2001; N. Smith et al. 2009; E. O'Gorman et al. 2015).

A dust- κ -like mechanism is also appealing because it simultaneously predicts the chromatic behavior of the LSPs

and could explain IR LC dips apparently modulated by increases and decreases in dust activity in front of the star (I. Soszyński 2007; I. Soszyński et al. 2021; J. R. Percy & M. H. Shenoy 2023). Such a pulsation, if it is indeed dragging the whole star, would also explain the typical LSP LC–RV phase offset, with the LSP luminosity minimum (indicating more dust) occurring shortly after the maximum in the modulated stellar RV (indicated by a low but increasing photospheric RV).

Ultimately, the ability of such a pulsation out at 3 R to adequately modulate the RV at the level of $\approx \pm 2.5$ km s⁻¹ at the stellar surface is the primary point of tension for the dust- κ theory. As pointed out by P. R. Wood et al. (2004a, 2004b), if dust is being created and ejected via a dust- κ mechanism, this phenomena would occur primarily outside the stellar photosphere and it is unclear how the deeper photospheric layers could be dragged enough to cause the RV amplitude modulations seen in LSPs, and this argument extends also to Betelgeuse. Moreover, changes in L and the optical stellar photosphere R would be accompanied by large changes in T_{eff} . We note that this was not seen even in the Great Dimming's extreme dust ejection near LSP minimum (M. Montarges et al. 2021), during which Betelgeuse's $T_{\rm eff}$ cooled slightly but remained at $T_{\rm eff} \approx 3600 \pm 25$ K (E. M. Levesque & P. Massey 2020). This low variation in $T_{\rm eff}$ is consistent with other LSP variables, which show little modulation in $T_{\rm eff}$ (P. R. Wood et al. 2004b). Finally, though Betelgeuse does exist within a surrounding dusty circumstellar medium, it should be noted that some LSP stars show little evidence for large circumstellar dust shells to begin with (K. H. Hinkle et al. 2002; E. A. Olivier & P. R. Wood 2003). While some kind of externally sourced pulsation remains capable in theory of reconciling the RV phase and the LSP, there is no clear way to do this without large corresponding changes in $T_{\rm eff}$.

4.8. Hypothesis 8: Modulation by a Companion

In this section, we overview the ways in which a companion could induce an LSP (see, e.g., P. R. Wood et al. 1999, 2004b; A. Retter 2005; I. Soszyński 2007; I. Soszyński et al. 2021; J. R. Percy & M. H. Shenoy 2023, and discussions and references therein). This family of solutions is the generally favored mechanism for producing LSPs, as this class of scenarios naturally explains the long timescale and steady period as the orbital time of the companion. As discussed in Section 2, the existence of a P-L relation for LSPs is not an intrinsic problem, as orbital architecture is sensitive to the stellar mass and radius. A remaining point of tension is the relatively high fraction of LPVs with LSPs and RV modulations compared to main-sequence stars (C. P. Nicholls et al. 2009), which can be addressed by appealing to mass growth of the orbiting body (e.g., M. Livio & N. Soker 1984; see the discussion in Section 5 of I. Soszyński et al. 2021). At least regarding RSGs, the observed binary fraction is very high for massive stars (H. Sana et al. 2012; S. E. de Mink et al. 2013), and this fraction does not include undetected lower mass companions (we return to this in Section 5.2).

4.8.1. Hypothesis 8a: Tidally Induced Oscillations

Tidally induced oscillations are another form of nonradial oscillations (see Section 4.6) that emerge in highly nonadiabatic conditions (see, e.g., A. Bunting et al. 2019; M. Sun et al.

⁷ In order to achieve a modulated RV signal, near-stellar-photosphere material would need to take part in the oscillation, so the stellar mass is expected to set the mean density unless there is very appreciable mass within the dust shell.

2023). In the case of a companion inducing modes on Betelgeuse via tidal forces, it is the companion's orbital timescale that could modulate the RV variations, but an oscillation of the star or system that determines the luminosity fluctuations. If we consider tidally driven modes induced on Betelgeuse by a companion, these modes are still acoustic p-modes acting over the surface of Betelgeuse and are therefore limited by its radius (R/c_s) . Considering the case of a severely tidally distorted Betelgeuse, because $R/c_s = t_{\rm dyn}$ at the surface, to distort the star substantially in a Roche potential would require a very short orbital period on the order of the FM. As such, tidally driven modes in the star itself cannot have significantly lower frequencies than the FM.

If, on the other hand, we consider a scenario in which the potential of the orbital system—Betelgeuse and its companion -drives a pulsational mode that acts over the radius of the whole system (rather than Betelgeuse alone), it is unclear what would be pulsating. If the oscillating medium is a steady-state dust shell encompassing both bodies, then we encounter difficulties providing a physical justification for a pulsation in such a low-density environment (see also Section 4.7). There remains the possibility that such an oscillation might mediate the properties of the dust, thereby modulating the luminosity and chromatic behavior. If the orbit provides RV modulation in 1:1 resonance with an induced oscillation period, this might explain why there could be a sizeable RV modulation with a relatively steady $T_{\rm eff}$. In general, however, this scenario would not prefer any particular phase relationship between the LSP and the RV, since a pulsating dust shell modulating the luminosity would not know about the observer's direction. In either case, tidally induced oscillations do not provide a clean explanation for the LSP.

4.8.2. Hypothesis 8b: Occultation

The current preferred hypothesis for LSPs posits that a lowmass companion is dragging a cloud of dust and gas along the observer's line of sight, temporarily blocking the view of the star and causing the luminosity minimum (see, e.g., P. R. Wood et al. 1999, 2004b; I. Soszyński 2007; I. Soszyński & A. Udalski 2014; I. Soszyński et al. 2021; J. R. Percy & M. H. Shenoy 2023). This theory is appealing as it (1) naturally explains a timescale longer than the FM, (2) allows for RV modulation on the LSP timescale, (3) without substantial changes in $T_{\rm eff}$, and (4) explains dust-like chromatic behavior. As discussed in detail by I. Soszyński et al. (2021), a compelling piece of evidence for dust modulation on an orbital timescale as an explanation for the LSP phenomenon comes from inspecting the shape of the LSP LCs. These vary in the characteristics of their luminosity fluctuations, from narrower dips commensurate with small orbiting dust blobs, through deep periodic signals consistent with much larger or more complex orbiting dusty bodies. As discussed in Section 2, there is no significant tension between a companion hypothesis and the existence of a P-L relation; in fact, this succinctly explains why sequence D in our Figure 1 and Figure 2 of I. Soszyński et al. (2021) extends from the sequence of lower-luminosity eclipsing binaries (sequence E).

A diversity of LSP amplitudes would be expected for different inclination angles and companion/dust cloud properties, and this model can explain cases where there is no detectable RV signal by invoking a very high mass ratio. However, the occultation hypothesis predicts that when RV

modulation is present on the LSP timescale, one should infer the orbiting companion to be somewhere along the observer's line of sight, i.e., the star's v_r should be near average and accelerating toward the observer near luminosity minimum, at a phase offset of $\phi \approx +\pi/2$ or $-3\pi/2$ (see Figure 3).

Unfortunately, this prediction does not hold for Betelgeuse with its LSP–RV phase offset of -0.63π . This is almost 180° out of phase with what would be expected for dust gravitationally bound to an orbiting body or at the L1 Lagrange point and still $\approx\!120^\circ$ out of phase with dust sitting the L4 or L5 Lagrange points. The occultation hypothesis is also in tension with the RV phases for the majority of the Gaia sample shown in Figure 3 and discussed in Section 3. Thus while the orbiting dusty body hypothesis can explain the RV amplitude and LC period in Betelgeuse, it does not explain their phase offset.

4.8.3. Hypothesis 8c: Circumstellar Modulation Near a Companion

The tension between the dusty companion hypothesis and the RV-LC phase offset requires reevaluating the broader physical picture. From Figure 2, the phase difference between the LC and RV modulation favors a scenario in which the photosphere begins to move away from the observer near the time of LSP luminosity minimum. For this to be caused by a companion, the companion must be 180° out of phase with the dust that induces the brightness minimum of the LSP. Thus we propose a new scenario: a companion whose orbital period sets the timescale of the LSP and RV fluctuations, and whose presence modulates, removes, eliminates, or changes the optical depth of any potentially dusty material in its vicinity, rather than dragging a trailing cloud of dusty material. There are multiple ways in which this might occur, including, for example, dynamically perturbing the potential of the dusty medium or through irradiation.

For this scenario to be feasible, there must be material for the companion to interact with, and the timescale over which the circumstellar matter replenishes and enters into proximity with the companion must be shorter than the orbital period. Both of these conditions appear to be satisfied in Betelgeuse. As supported by observational measurements of material extending from the MOLsphere to many tens of stellar radii beyond, it is well established that dusty material exists outside the photosphere (N. Smith et al. 2009; P. Kervella et al. 2009, 2011; M. Montargès et al. 2014; E. O'Gorman et al. 2015; T. E. Dharmawardena et al. 2018; X. Haubois et al. 2019).

The connection between binarity, convection, pulsation, dust condensation, and mass loss has been explored by various groups in both simulations and observations (see, e.g., S. Höfner & H. Olofsson 2018 for a recent review in the context of AGB mass loss). Both 1D and 3D simulations of evolved cool giant stars exhibit dust-driven winds forming at a few times the stellar radius, seeded by (asymmetric) material which gets shocked and levitated by the pulsating stellar surface (see, e.g., B. Freytag & S. Höfner 2008; S. Liljegren et al. 2016, 2017, 2018; B. Freytag et al. 2017; S. Bladh et al. 2019a, 2019b; L. Siess et al. 2022; U. P. Steinwandel et al. 2022; B. Freytag & S. Höfner 2023; J. Wiegert et al. 2024). The outflows in these works exhibit a wide range of circumstellar densities and mass-loss rates that depend on properties near the stellar surface, such as the pressure scale height, temperature, pulsation period, and degree of asymmetry

 Table 2

 Summary of Hypotheses for Betelgeuse's Long Secondary Period

Hypothesis	Section	Timescale	Properties of RV	Low Variation in $T_{\rm eff}$	Dust-like Chromaticity	LC-RV Offset	Persistence
Misidentified FM	4.1	√ +	X	?	-	?	√ +
Giant convective cells	4.2	✓	?	✓	-	-	X
Mode interactions	4.3	X	X	-	-	-	X
Rotation	4.4	X	✓	?	?	✓	√ +
Magnetism	4.5	X	-	X	X	?	?
Nonradial pulsation	4.6	√ +	✓	?	?	?	X
Dust κ	4.7	√ +	√ +	X	$\checkmark+$	√ +	✓
Binarity: tidal	4.8.1	X	√ +	?	?	?	√ +
Binarity: occultation	4.8.2	√ +	√ +	\checkmark +	\checkmark +	X	√ +
Binarity: dust modulation	4.8.3	√ +	√ +	√ +	√ +	√ +	√ +

Note. Physical properties and observational constraints/pieces of information we have for Betelgeuse are listed across the top row. A check mark - plus (\checkmark +) pair underneath one of these pieces of information indicates that the corresponding hypothesis, given in the left-most column, is supported by that piece of information. A check mark (\checkmark) indicates consistency. A question mark (?) indicates that the relationship between the hypothesis and constraint is unclear or unknown. A dash (-) means that the hypothesis does not provide any information on the constraint. An X indicates that the hypothesis is contradicted by the constraint.

(as well as composition; see, e.g., A. I. Karakas & J. C. Lattanzio 2014; J. Lattanzio & A. Karakas 2016).

Likewise, observations indicate a correspondence between the onset of dusty winds and different pulsation sequences (e.g., I. McDonald & M. Trabucchi 2019; J. Yu et al. 2021). LSPs have long been associated with dusty activity, as P. R. Wood & C. P. Nicholls (2009) found increased midinfrared emission with no difference in color for RGB stars with LSPs compared to those without, interpreted to indicate the presence of dust in a clumpy or disk-like configuration. It has also been shown in hydrodynamic simulations of AGB star winds that a companion may modify the circumstellar matter formed by dusty outflows (S. Maes et al. 2021), with differing geometry depending on the properties of the outflow and companion.

Two important timescales may set the launching of periodic or stochastic outflows which might turn into dusty fodder: pulsations and convection. The pulsation timescale (FM or O1) is necessarily shorter than the LSP, and the coupling of nearsonic, large-scale convection in a pulsating envelope has been hypothesized to drive stellar winds (S.-C. Yoon & M. Cantiello 2010). Similarly, the convective motions themselves may lead to steepening shocks in the atmosphere. This may stratify material beyond the stellar photosphere, well past the dust formation radius, with variations changing over the convective turnover time (J. Fuller & D. Tsuna 2024). A timescale for this process can be estimated by considering motions in the deep interior, following Equation (B4) of J.-Z. Ma et al. (2024)

$$t_{\text{turnover}} \sim \frac{R}{v_c} \sim 0.8 \text{yr} \left(\frac{R}{800 R_{\odot}}\right) \left(\frac{T_{\text{eff}}}{3600 \text{ K}}\right)^{-\frac{4}{3}} \rho_{s,-9}^{\frac{1}{3}},$$
 (9)

where $\rho_{s,-9}$ is the density at the optical photosphere $(\rho/10^{-9} \text{ g cm}^{-3})$, or surface timescales much shorter than that (see the discussion in Appendix B of J.-Z. Ma et al. 2024). It is also known that for particularly extreme dust ejection events, such as the Great Dimming (M. Montarges et al. 2021; A. K. Dupree et al. 2022; J. Drevon et al. 2024) a major dust cloud forms and passes on timescales shorter than the LSP (see the extensive discussion in M. MacLeod et al. 2023).

The modification we are presenting to the dust-modulating-companion scenario originally discussed in, e.g., P. R. Wood et al. (1999), I. Soszyński (2007), I. Soszyński & A. Udalski (2014), and I. Soszyński et al. (2021), is appealing for the four

reasons mentioned in Section 4.8.2 (timescale, RV modulation, low variance in $T_{\rm eff}$, and chromaticity), with the additional benefit that it explains the phase offset in Betelgeuse, as well as many of the Gaia LSP variables (Figure 3).

A dust-modulating companion also leaves open the possibility of secondary eclipses to be seen in the IR, which represent strong evidence for the binarity scenario in other cases (I. Soszyński et al. 2021). The primary difference is that the companion would be $\approx\!180^\circ$ out of phase with the bulk of the circumstellar dust rather than dragging the dust along as in the occultation scenario. This phase difference would potentially but not necessarily yield differences in the (highly uncertain) expected dust geometry, depending in part on whether the dust modulation is dynamical or radiative in nature.

We note that elimination or dispersal of dust near an orbiting body need not be the explanation for all LSP variables. Many LSP variables do show steady amplitudes and periodic narrow LC dips (I. Soszyński et al. 2021), and at least a few show RV modulation phases consistent with luminosity drops when the companion would be in front of the star. It is likely that the mass, luminosity, and $T_{\rm eff}$ of the companion, as well as the replenishment timescale of material provided by the star, may determine whether the system drags and condenses dust along its orbit or creates an underdensity in its surroundings. We leave it to future work to determine the exact conditions under which each orbitally modulated LSP/RV phase scenario (occultation, dynamical dispersal, accretion, irradiation, etc.) could arise.

We thus conclude that circumstellar dust modulation by a companion is the most plausible explanation for the LSP in Betelgeuse. Within this framework, we can use the observational data available to estimate the properties of a companion consistent with the RV and RV–LC phase difference. This companion is hereafter referred to as α Ori B. The properties (Section 5) and detectability (Section 5.2) of α Ori B are discussed subsequently.

4.9. Summary of Hypotheses

Table 2 provides a quick-look reference for the explanatory power and limitations of each theory discussed in this section.

 $^{^{8}}$ "B" stands for Betelbuddy.

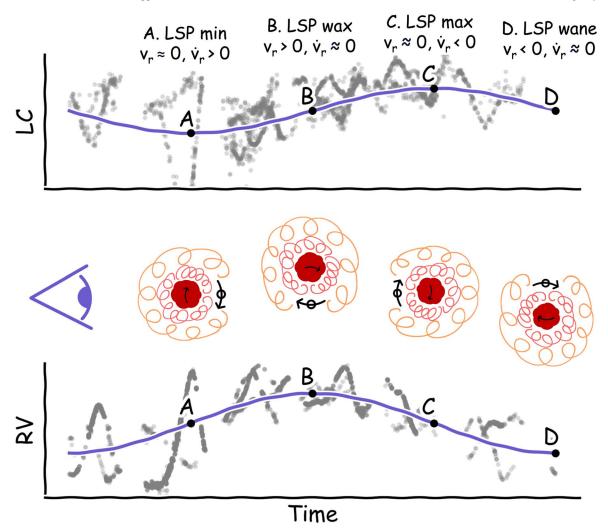


Figure 4. Schematic of the dust modulation by a companion as discussed in Section 4.8.3 over the course of an orbit. The diagram in the center shows four orientations of the companion (black circle) as well as Betelgeuse (solid red blob) and some circumstellar gas and dust (curly lines). The arrows represent the motion of the two objects. This is compared to the period in the LC (upper panel) and RV modulation (lower panel). The phase-folded data from Figure 2 are overplotted in gray, with the four highlighted phases labeled as A, B, C, and D. These approximately correspond to (A) the minimum brightness (increasing RV, with the stellar photosphere accelerating away from the observer), (B) increasing brightness (approximate RV maximum), (C) maximum brightness (decreasing RV, star accelerating toward the observer), and (D) decreasing brightness (minimum RV). The Great Dimming of 2020 can be seen in the phase-folded LC near LSP minimum (A). When α Ori B is behind Betelgeuse relative to the observer's line of sight as indicated by the RV (configuration A), circumstellar dust is able to obscure the system. When α Ori B is in front of Betelgeuse (configuration C), dust unaffected by α Ori B is (at least partially) eclipsed by Betelgeuse.

5. Companion as the Long Secondary Period in Betelgeuse

In Section 4, we argued that the most plausible explanation for the LSP in Betelgeuse is a low-mass companion (α Ori B) that impacts the dust in its vicinity, corresponding to a brightness increase when the companion is in view, a novel revision of the scenario described by I. Soszyński et al. (2021). Figure 4 gives a schematic diagram of the α Ori system proposed in Section 4.8.3 over one cycle of the LSP, and illustrates the approximate location of α Ori B at various points in the phase-folded LC and RV cycles from Figure 2: (A) increasing RV at LSP minimum (α Ori B behind Betelgeuse), (B) maximum RV at LSP median (α Ori B on the limb moving into view), (C) decreasing RV at LSP maximum (α Ori B in view), and (D) minimum RV at LSP median (α Ori B on the limb moving out of view). In the remainder of this section, we constrain the orbital properties of the posited α Ori B, and explore the implications of such a companion.

5.1. Properties of the Companion

From the RV data we estimate the mass of $\alpha\,\mathrm{Ori}\,\mathrm{B}$ via the binary mass function

$$f = \frac{M_2^3 \sin^3 i}{(M_1 + M_2)^2} = \frac{P K^3}{2\pi G},\tag{10}$$

where K is the velocity amplitude, $P=2169\pm5.3$ days is the LSP period from the RV observations of T. Granzer et al. (2022), and M_1 is the present-day mass estimate of $18\pm1~M_{\odot}$ from M. Joyce et al. (2020). For simplicity, we assume a circular orbit. This assumption is further justified given the expected effects of dust reducing eccentricity, investigated primarily in the context of planets in dusty disk environments by, e.g., Y.-P. Li et al. (2019) and G. A. L. Coleman et al. (2022). This gives us a lower mass limit of $M_2 \sin i = 1.17 \pm 0.07~M_{\odot}$. This value is an order of magnitude larger than the mass estimates calculated for LSPs in

RGBs with RV constraints, which are typically in the $0.1~M_\odot$ or less range, i.e., closer to brown dwarfs than to dwarf stars (C. P. Nicholls et al. 2009). In order to cause substantial modulation over the course of an orbit, we assume that a relatively low inclination relative to our line of sight (or a high inclination i relative to the plane perpendicular to our line of sight, as defined conventionally for binary stars and exoplanets) is needed for any interaction with the circumstellar dust to be observable from our vantage point. Therefore, we estimate that the mass of α Ori B is unlikely to exceed $1.5~M_\odot$, or $2~M_\odot$ at most with a vertically extended cloud.

Using this mass constraint, we calculate the orbital separation assuming a Keplerian orbit

$$P = 2\pi \sqrt{\frac{a^3}{G(M_1 + M_2)}},$$
(11)

which recovers an orbital separation of $a = 1850 \pm 70 \ R_{\odot}$ assuming the 18 ± 1 M_{\odot} present-day mass of Betelgeuse estimated by M. Joyce et al. (2020). Using their stellar radius of $R = 764^{+116}_{-62} R_{\odot}$ yields an orbital distance of $a = 2.43^{+0.21}_{-0.32} R_{*}$. This is well outside of the CO₂-H₂O MOLsphere described by M. Montarges et al. (2021), which extends to $\approx 1.2 R_*$. It also places the L1 Lagrange point at $\approx 1380 R_{\odot}$, or $\approx 1.8 R_{*}$. In this orbital configuration, the surface of Betelgeuse is not expected to deform significantly, as the Roche radius for this orbit is $\approx 1100 R_{\odot}$, and the equipotential corresponding to 764 R_{\odot} is nearly spherical. From the calculated separation, we can estimate a transit probability of $P = R_*/a = 41^{+6}_{-3}\%$, and a corresponding minimal inclination of $i_{min} = 66^{+2}_{-4}$ degrees for a grazing transit of α Ori B (where an inclination of 90° means an edge-on orbit). Therefore, even with an extended dust feature that can reach higher inclinations, our assumption of low inclination relative to the observer's line of sight is justified.

It remains unclear from these orbital parameters alone whether α Ori B is able to modulate dust. Any irradiation effects will depend on the companion's age, outgoing radiation field, and the dust properties, which dynamics alone cannot recover (see further discussion in Section 5.2). From dynamical arguments, one can calculate the Hill sphere of the companion star, which approximates its sphere of gravitational influence

$$R_{\rm H} \approx a_3^3 \sqrt{\frac{M_2}{M_1 + M_2}}$$
 (12)

This gives $R_{\rm H} \approx 0.25$ –0.35 a within the likely ranges for α Ori B's mass, or 60%–80% of the radius of Betelgeuse. This is at least a plausible angular cross section to subtend over which one might see modulation.

5.2. Observability of the Companion

Even at its highest plausible mass—say $M_2\lesssim 2~M_\odot$ —it would be nearly impossible to detect α Ori B close to such a luminous and intrinsically variable star (the average brightness of Betelgeuse hovers near $L\sim 10^5~L_\odot$) except in some exotic and improbable scenarios (see Section 5.2.1). Even adopting an optimistic $10~L_\odot$ for α Ori B, the luminosity contrast would still be $\approx 10^{-4}$, likely undetectable in integrated light. This challenge is exacerbated by the fact that Betelgeuse's intrinsic variability from

Parameter	Value	Reference
Radius of Betelgeuse	$764^{+116}_{-62}R_{\odot}$	M. Joyce et al. (2020)
Mass of Betelgeuse	$18\pm1~M_{\odot}$	M. Joyce et al. (2020)
Radius of Betelgeuse	$764^{+116}_{-62}R_{\odot}$	M. Joyce et al. (2020)
Orbital period	$2169 \pm 5.3 \text{ days}$	T. Granzer et al. (2022);
		D. Jadlovský et al. (2023)
$M \sin i$ of α Ori B	$1.17\pm0.07~M_{\odot}$	This work
Orbital separation a	$1850 \pm 70~R_{\odot}$	This work
DD/MM/YYYY of next RV min	06/12/2024	This work
DD/MM/YYYY of next RV max	26/11/2027	This work
DD/MM/YYYY of second RV min	15/11/2030	This work
DD/MM/YYYY of second RV max	04/11/2033	This work

convection and pulsations entails ≈ 1 mag fluctuations in the V-band (see our Figure 2), with intrinsic fluctuations on the order of more than $\sim \pm 10^4 L_{\odot}$, at least 1000 times the intrinsic brightness of α Ori B.

Spectral differencing at different phases would be another possible avenue for detection, but again, subtle changes in the $T_{\rm eff}$ of Betelgeuse and changes on the FM timescale would overwhelm variations in spectra unless the companion were substantially hotter than Betelgeuse. At its hottest, a 2 M_{\odot} star might be spectral class F, corresponding to a $T_{\rm eff}$ of $\approx 6000-7000$ K. A companion of this temperature would only just barely be visible on the Wien tail in the UV (a 7000 K blackbody outshines a $10^4 \times$ brighter, 3600 K blackbody only above 1.7×10^{15} Hz, or below ≈ 1760 Å), and realistically, this is a drastic overestimate of the temperature of α Ori B.

5.2.1. Exotic Scenarios

While the companion's mass and proximity to a massive star might lead one to speculate that it may be a neutron star or other exotic compact body, as far as the authors of this study are aware, no such detections have been made (J. Posson-Brown et al. 2006; V. L. Kashyap et al. 2020). The current lack of X-ray evidence notwithstanding, there are a few reasons not to entirely ignore a neutron-star-as-companion scenario. First, it is more common than not that high-mass stars such as Betelgeuse are born as binary or even triple systems (H. Sana et al. 2012; S. E. de Mink et al. 2013; S. Toonen et al. 2018, 2020, 2022, S. S. R. Offner et al 2023), many of which will produce runaway stars when the most massive star in the system explodes (e.g., J. J. Eldridge et al. 2011; E. Zapartas et al. 2021). Second, the anomalous proper motion of Betelgeuse (e.g., G. M. Harper et al. 2008) still requires explanation, and a neutron star companion could provide one. In that scenario, the progenitor to a neutron star born at the same time as Betelgeuse must have been more massive than Betelgeuse in order to die earlier in a supernova explosion. The past supernova explosion of Betelgeuse's companion would have then been energetic enough to provide the necessary "kick" that sent Betelgeuse along its present observed trajectory, with the binary widening but without disrupting the system (M. Renzo et al. 2019). Future X-ray observations scheduled at favorable epochs might

rule this out conclusively. Such an experiment could also help characterize the presence of a possible corona around a noncompact companion, which might yield insight into the exact mechanism for interaction with any circumstellar dust.

Using an approximate age for Betelgeuse of ~ 10 Myr, and assuming Betelgeuse and its companion are conatal, it is possible that α Ori B could be a low-mass, pre-main-sequence star hosting an accretion or protoplanetary disk. While this could be bright enough to detect, given typical disk lifetimes between 10^5-10^7 yr (E. Fiorellino et al. 2023), the probability of catching the system in this particular configuration is exceedingly low. The authors are likewise unaware of any existing observational evidence of this scenario.

5.2.2. Observability under Normal Conditions

For spectral differencing or photometry, the closeness of the orbit can be exploited, since the probability of the companion being eclipsed from our vantage point is $P=R_*/a\approx 0.41$. Therefore, an eclipse in the UV passbands would be potentially detectable. Future space-based UV spectroscopic missions such as UVEX (S. R. Kulkarni et al. 2021) would be well positioned to investigate this. However, one still would have to contend with the length of an eclipse. As for the orbital parameters and a near-circular orbit, the approximate time for α Ori B to cross the disk of Betelgeuse is ≈ 300 days, i.e., longer than an observing season, and comparable to the FM and O1 pulsation periods.

Another possibility is to inspect the shape of evolving asymmetries in submillimeter observations of the dusty region around Betelgeuse using an instrument like the Atacama Large Millimeter/submillimeter Array (ALMA). There is indeed substantial asymmetry in the dust observed near the radius of the predicted orbital separation of α Ori B (e.g., A. M. S. Richards et al. 2013; E. O'Gorman et al. 2017, 2020; P. Kervella et al. 2018).

As the sensitivity and achievable luminosity contrast of instruments with powerful coronagraphs and extreme adaptive optics systems designed for planet hunting and other purposes improve, we are optimistic that in the future such a companion will be detectable, and in the meanwhile we emphasize this system will make for an interesting target for creative observers.

For future targeted observations, the RV phase can be used to predict where α Ori B will be relative to the star over the next LSP cycle and beyond. Directly observing a transit of α Ori B is impossible given Betelgeuse's intrinsic periodic and stochastic variability from convection and pulsations on shorter timescales than the transit. However, the times when α Ori B is near the limb could in theory reveal its presence and stellar properties if observed at sufficiently high contrast and spatial resolution. Given the LSP period of 2170 days, the following are the upcoming epochs where α Ori B would be near maximum separation:

- 1. Min RV: JD 2460651, 2024 December 06,
- 2. Max RV: JD 2461736, 2027 November 26,
- 3. Min RV: JD 2462821, 2030 November 15, and
- 4. Max RV: JD 2463906, 2033 November 04,

with syzygy halfway in between.

In the absence of instrumentation breakthroughs enabling extremely high luminosity contrast direct imaging for stars as bright as Betelgeuse ($L \sim 10^5 L_{\odot}$), we believe the best chance for observability or falsification is with repeated targeted radio interferometric observations continuously throughout the LSP

cycle. These studies should look specifically for patterns in the dust modulation and asymmetry correlated with α Ori B's expected orbital separation.

A similar observing strategy was undertaken by E. O'Gorman et al. (2015), who took Very Large Array measurements at 0.7, 1.3, 2.0, 3.5, and 6.1 cm at multiple different phase points along the LSP over a 4 yr cycle (in addition to single-epoch observations by J. Lim et al. 1998 4 yr prior). Their Figure 1 does indicate some time-dependent modulation of an asymmetric circumstellar envelope visible in the 0.7 cm interferometric data around $\approx\!50$ mas, but it is far from conclusive evidence, as an 8 yr time span entails measurements during multiple different LSP cycles (orbit of α Ori B). While we do expect intrinsic diversity in dust structures on a replenishment timescale commensurate with the FM as the FM interacts with the large-scale convection, α Ori B would cause a systematic modulation in the circumstellar dust (the proposed mechanism for the LSP itself).

If an apparent underdensity of dust migrates around the star on the LSP cycle, and if that matches the points in the LSP cycle where α Ori B should be on the limb versus transiting Betelgeuse versus in opposition, this would lend strong evidence to the existence of α Ori B as proposed. Such a finding would also further constrain the system's orbital plane and inclination, the companion's stellar properties, and the mechanism by which α Ori B interacts with the dust.

6. Conclusions

In this study, we have demonstrated that the most likely explanation for the prominent 2170 day periodicity observed in Betelgeuse is a low-mass, binary companion, dubbed α Ori B, that modulates dust. The proposed orbital picture leads to reduced obfuscation (higher apparent stellar L) when α Ori B is in transit.

In Section 2, we reviewed the variability phenomenon known as LSPs present in roughly 30% of all LPV stars and in Betelgeuse specifically. In Section 3, we compiled and presented new data (Figure 2) comparing Betelgeuse's LC and RV cycle side by side, and characterized the phase offset between them. We showed that the phase offset present not only in Betelgeuse, but in the majority of Gaia LSP stars, contradicts the physical picture set by the prevailing theory for binarity as the driver for LSPs proposed by I. Soszyński et al. (2021).

In light of the tension introduced by the RV–LC phase offset, we extensively investigated the explanatory power of every hypothesis proposed for LSPs in the literature as applied to Betelgeuse. Section 4 covered possibilities ranging from large-scale convection, magnetism, mode interactions, non-radial pulsations, and exotic physics, but only converged on one viable explanation: Betelgeuse's LSP is caused by a low-mass companion, α Ori B, in a dusty environment.

In Section 5, we calculated physical properties of the companion and the α Ori orbital system as constrained by existing observations. A summary of these parameters is provided in Table 3. We discussed why α Ori B has not been detected before, commented on exotic physical scenarios that would be theoretically observable, discussed practical limitations on the companion's detectability, and described the advances in method, technique, and instrumentation needed to detect it in the future.

 $^{^9}$ At maximum separation, α Ori B will be at ${\approx}52$ mas for a stellar optical photosphere diameter of 43 mas).

While our work was in the refereeing process, M. MacLeod et al. (2024) independently found astrometric evidence that a companion scenario can explain Betelgeuse's LSP, focusing their efforts on dissecting Betelgeuse's long baseline RV observations. They recovered similar orbital parameters and a slightly lower mass ($M \lesssim 1~M_{\odot}$) due to a smaller inferred RV amplitude.

The confirmation of α Ori B would have far-reaching implications for Betelgeuse and its evolutionary future. Betelgeuse is expected to explode as a Type IIPlateau supernova, and when it does, it could appear nearly as bright as the quarter moon (J. A. Goldberg et al. 2020a). There is substantial uncertainty in the expected early supernova luminosity evolution due to the unknown status of Betelgeuse's pulsation phase at the time of explosion (J. A. Goldberg et al. 2020b; Hsu et al. 2024) and the properties of the near-surface material (e.g., T. Moriya et al. 2011; V. Morozova et al. 2017, 2018; T. J. Moriya et al. 2018; D. Hiramatsu et al. 2021; A. Kozyreva et al. 2022; T. J. Moriya et al. 2023; W. V. Jacobson-Galán et al. 2024).

The presence of dense circumstellar material is of reinvigorated interest after the recent SN 2023ixf, the closest corecollapse event of the decade, which showed strong signatures of early interaction in an asymmetric circumstellar medium (e.g., D. Hiramatsu et al. 2023; G. Hosseinzadeh et al. 2023; W. V. Jacobson-Galán et al. 2023; N. Smith et al. 2023; R. S. Teja et al. 2023; K. A. Bostroem et al. 2024; G. Li et al. 2024; L. Martinez et al. 2024; T. J. Moriya & A. Singh 2024; A. Singh et al. 2024; E. A. Zimmerman et al. 2024) around a pulsating RSG progenitor (e.g., J. E. Jencson et al. 2023; C. D. Kilpatrick et al. 2023; M. D. Soraisam et al. 2023; D. Xiang et al. 2024). Moreover, supernova remnants are now being observed with unprecedented resolution in the era of JWST (e.g., recent work by T. Temim et al. 2024; D. Milisavljevic et al. 2024), and the proposed observations of Betelgeuse's surrounding environment, whether or not they support the presence of α Ori B, will be valuable in constraining the expected level and geometry of circumstellar asymmetries that may imprint on the remnant morphology (A. Polin et al. 2022; S. Mandal et al. 2023, 2024). If the existence of α Ori B is confirmed and a progenitor identified, one could also predict its own future evolution in the context of Betelgeuse's eventual explosion. Such simulations have recently been carried out in the case of Type Ia supernovae with a surviving companion (E. B. Bauer et al. 2019; A. Bhat et al. 2024; T. L. S. Wong et al. 2024).

Observations of Betelgeuse have identified photometric variations on a 30 yr period consistent with a rotational $v \sin i \approx 5$ km s⁻¹ (M. Joyce et al. 2020), which for an inclination angle of 20° recovers an equatorial velocity of 15 km s⁻¹ (see A. K. Dupree et al. 1987; R. L. Gilliland & A. K. Dupree 1996; H. Uitenbroek et al. 1998; P. Kervella et al. 2009, 2018; and the review by J. C. Wheeler & E. Chatzopoulos 2023). This has led to speculation that Betelgeuse may be a merger product (e.g., J. C. Wheeler et al. 2017; E. Chatzopoulos et al. 2020; S. Shiber et al. 2024). This hypothesis was invoked to account for fast envelope rotation, which would not survive the spin-down as Betelgeuse ascended up the RSG branch in a single-star evolutionary scenario. Although the large-scale convective envelope itself might be the source of this RV signal (J.-Z. Ma et al. 2024), if the apparent RV dipole signal persists at a consistent inclination or at higher ALMA resolution, another possible explanation might be angular

momentum transferred from the orbit of α Ori B, which could be informed by further constraining the stellar mass and properties of α Ori B.

In this picture, it is not purely a coincidence that the Great Dimming of 2020 (e.g., A. K. Dupree et al. 2020, 2022; M. Montarges et al. 2021; J. Drevon et al. 2024) occurred near LSP minimum. As the opening angle of such an ejection is expected to be large if caused by a large pressure perturbation from convection in the interior (M. MacLeod et al. 2023), a transiting companion would likely disrupt its path. However, a companion on the other side of Betelgeuse's potential would likely not interact. One may speculate that dusty mass loss could be funneled through the orbit's L3 Lagrange point, though dynamical modeling including gas—dust interactions are necessary to quantitatively evaluate this claim.

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Appendix Data Tables

In this appendix, we present the following data in numerical format. Table 4 lists the brightnesses, distances, and periods for the Galactic supergiant stars from Figure 1. Measured periods P1, P2, and P3 correspond to the first, second, and third highest-amplitude periods, with error estimates denoted by e. Table 5 lists the phase offset values we calculated for the stars presented by C. P. Nicholls et al. (2009), whereas Tables 6 and 7 contain the phase offset for the subset of Gaia LSP candidates that we include in Figure 3.

Table 4
Red Supergiant Periods Identified by L. L. Kiss et al. (2006)

ID	K_s	d	M_K	P_1	eP ₁	P_2	eP ₂	P_3	eP ₃	Reference
	(mag)	(pc)	(mag)	(days)	(days)	(days)	(days)	(days)	(days)	
SS And	0.971	592 ⁺¹⁸ ₋₂₀	$-7.89^{+0.06}_{-0.07}$	159	17					(1)
NO Aur	3.729	1183^{+51}_{-60}	$-6.64^{+0.09}_{-0.11}$	362	11	38.4	0.3			(1)
VY CMa	0.291	850^{+2259}_{-157}	$-9.36^{+2.82}_{-0.44}$	1600	190					(1)
RT Car	1.500	2134^{+121}_{-99}	$-10.15^{+0.12}_{-0.10}$	201	25	448	146			(1)
CL Car	1.539	2421^{+148}_{-126}	$-10.38^{+0.13}_{-0.12}$	490	100	229	14	2600	1000	(1)
EV Car	0.788	2424^{+262}_{-227}	$-11.13^{+0.22}_{-0.21}$	276	26	820	230			(1)
IX Car	1.884	2188^{+86}_{-91}	$-9.82^{+0.08}_{-0.09}$	408	50	4400	2000			(1)
TZ Cas	1.939	2335^{+147}_{-157}	$-9.90^{+0.13}_{-0.15}$	3100	1000					(1)
PZ Cas	0.781	2586^{+286}_{-254}	$-11.28^{+0.23}_{-0.22}$	850	150	3195	800			(1)
ST Cep	1.644	3974^{+356}_{-315}	$-11.35^{+0.19}_{-0.18}$	3300	1000					(1)
μ Cep	-1.620	1818^{+1039}_{-485}	$-12.92^{+0.98}_{-0.67}$	860	50	4400	1060			(3)
T Cet	-0.808	260^{+23}_{-18}	$-7.88^{+0.18}_{-0.16}$	298	3	161	3			(2)
RW Cyg	0.640	1649^{+124}_{-105}	$-10.45^{+0.16}_{-0.14}$	580	80					(1)
AZ Cyg	1.288	2290^{+129}_{-115}	$-10.51^{+0.12}_{-0.11}$	495	40	3350	1100			(1)
BC Cyg	0.299	1727^{+150}_{-152}	$-10.89^{+0.18}_{-0.20}$	720	40					(1)
TV Gem	0.947	2344^{+1400}_{-558}	$-10.90^{+1.02}_{-0.59}$	426	45	2550	680			(1)
W Gem	1.850	1799^{+145}_{-107}	$-9.42^{+0.17}_{-0.13}$	353	24					(1)
BU Gem	0.806	1757^{+439}_{-306}	$-10.42^{+0.48}_{-0.42}$	2450	750					(1)
α Her	-3.511	110^{+19}_{-14}	$-8.72^{+0.34}_{-0.29}$	124	5	500	50	1480	200	(3)
W Ind	3.108	1256^{+84}_{-62}	$-7.39^{+0.14}_{-0.11}$	193	15					(1)
Y Lyn	-0.688	350^{+16}_{-11}	$-8.41^{+0.10}_{-0.07}$	133	3	1240	50			(1)
XY Lyr	-0.213	415^{+21}_{-18}	$-8.30^{+0.11}_{-0.10}$	122						(1)
α Ori	-4.378	168^{+28}_{-15}	$-10.51^{+0.33}_{-0.20}$	410	32	200	20	2100	200	(5)
S Per	1.123	2421^{+104}_{-96}	$-10.80^{+0.09}_{-0.09}$	813	60					(4)
T Per	2.581	2200^{+120}_{-128}	$-9.13^{+0.12}_{-0.13}$	2500	460					(1)
W Per	1.568	1746^{+152}_{-90}	$-9.64^{+0.18}_{-0.11}$	500	40	2900	300			(1)
RS Per	1.562	2419^{+343}_{-264}	$-10.36^{+0.29}_{-0.25}$	4200	1500					(1)
SU Per	1.455	2211^{+128}_{-120}	$-10.27^{+0.12}_{-0.12}$	430	70	3050	1200			(1)
XX Per	1.972	2277^{+233}_{-159}	$-9.81^{+0.21}_{-0.16}$	3150	1000					(1)
BU Per	2.194	2267^{+216}_{-162}	$-9.58^{+0.20}_{-0.16}$	381	30	3600	1000			(1)
FZ Per	2.482	2530^{+153}_{-140}	$-9.53^{+0.13}_{-0.12}$	368	13					(1)
VX Sgr	-0.122	1563^{+104}_{-92}	$-11.09^{+0.14}_{-0.13}$	754	56					(4)
AH Sco	0.415	1735^{+286}_{-200}	$-10.78^{+0.33}_{-0.27}$	738	78					(1)
α Sco	-4.100	170^{+35}_{-25}	$-10.25^{+0.40}_{-0.34}$	1650	640					(3)
CE Tau	-0.913	708^{+174}_{-117}	$-10.16^{+0.48}_{9.77}$	1300	100					(1)
W Tri	1.091	578^{+24}_{-24}	$-7.72^{+0.09}_{-0.09}$	107	6	590	170			(1)

Note. Distance references: (1) C. A. L. Bailer-Jones et al. (2021), (2) Gaia Collaboration et al. (2021), (3) F. van Leeuwen (2007), (4) M. J. Reid et al. (2019), and (5) M. Joyce et al. (2020).

Table 5
Phase Offsets between the Radial Velocity Measurements Published by C. P. Nicholls et al. (2009) and the OGLE-III *I*-band Lightcurves for Stars Where Those Are Available

OGLE ID	P_{LSP}	$\Delta\phi_{ ext{RV}-I}$	$e\Delta\phi$
	(day)		
LMC-LPV-55909	783.7	-1.07	0.21
LMC-LPV-55739	562.1	-1.04	0.38
LMC-LPV-55861	1007	-1.95	0.11
LMC-LPV-55565	810.2	-2.34	0.16
LMC-LPV-57329	1032	-2.22	0.48
LMC-LPV-56928	800	-1.21	0.15
LMC-LPV-56063	540	-3.16	0.43
LMC-LPV-57356	434.8	-1.74	0.17
LMC-LPV-57073	470.5	-1.72	0.21
LMC-LPV-58350	611.6	-2.17	0.13
LMC-LPV-58399	818.7	3.90	0.13
LMC-LPV-58174	640.9	3.96	0.11
LMC-LPV-59753	1048	4.36	0.29
LMC-LPV-59287	257.7	-3.02	0.46
LMC-LPV-60196	1139	-1.93	0.35
LMC-LPV-61999	404.3	-3.07	0.21
LMC-LPV-60643	535.8	-1.02	0.20
LMC-LPV-61577	720.5	-1.75	0.15
LMC-LPV-62722	715.8	-2.48	0.17
LMC-LPV-63825	849.5	-2.86	0.27

Table 6Phase Offsets between the Long-period Variable Radial Velocity Measurements Published in the Gaia Focused Product Release (Gaia Collaboration et al. 2023a) and
the G-band Gaia DR3 Lightcurves

Gaia DR3 ID	P _{LSP} (day)	$\Delta \phi_{\mathrm{RV}-G}$	$\mathrm{e}\Delta\phi$	Gaia DR3 ID	P _{LSP} (day)	$\Delta\phi_{\mathrm{RV}-G}$	$e\Delta\phi$
5366556864650293504	467.8	-3.56	1.98	4518782615952131200	413.4	-1.98	0.52
5245519394861788416	424.3	-3.38	1.95	4591864301979656960	384.0	-1.95	0.83
2030155380681518080	415.3	-3.09	1.70	1958845802441119360	445.3	-1.70	0.24
4877073701212505984	467.9	-3.07	1.62	5823469916709143808	433.2	-1.62	0.93
1009476541884049152	436.2	-3.00	1.53	5404420815320630528	561.6	-1.53	0.56
416537855493120896	592.8	-2.54	1.48	1863461622559594624	472.3	-1.48	0.73
5592948576556271360	567.5	-2.54	1.47	2030200671149815424	442.6	-1.47	0.37
5487656658716777984	523.9	-2.52	1.43	5823227714910793856	368.1	-1.43	0.27
4242144837569110656	560.2	-2.52	1.36	5819332488801340928	381.8	-1.36	0.28
5193827058256042752	780.7	-2.47	1.35	718681245623682176	446.5	-1.35	0.35
2940744561181222784	510.5	-2.46	1.31	5592924490378357632	427.0	-1.31	0.46
5393712362310861824	378.9	-2.46	1.21	2022032910328304128	488.3	-1.21	0.15
5365837715327919872	294.4	-2.44	1.20	2226627353963447552	507.6	-1.20	0.73
5193010395993757952	585.3	-2.42	1.18	6036139001931775360	403.9	-1.18	0.39
1863379262264189568	339.0	-2.42	1.18	413371051550885248	436.6	-1.18	0.27
4325121337971096704	325.6	-2.42	1.11	5842150894131928576	367.5	-1.11	0.23
6648842337535201152	304.8	-2.42	1.04	5615714067889118336	605.4	-1.04	0.37
5783448380630645760	462.0	-2.41	1.04	419317730125131904	434.7	-1.04	0.25
525948917547462272	770.1	-2.39	1.03	5464229059521244928	289.8	-1.03	0.41
3417134843227320192	814.3	-2.38	0.96	4325728161012091904	453.3	-0.96	0.44
5870612332427790464	328.5	-2.37	0.95	2223228905258736128	680.9	-0.95	0.94
5793428029206907136	466.0	-2.36	0.95	5836237308379605248	387.0	-0.95	0.32
4216847961220342400	353.1	-2.35	0.90	2057374688680289408	685.6	-0.90	0.91
2162840771749435904	701.0	-2.34	0.87	563548504362254464	547.5	-0.87	0.32
6065282485339565440	694.1	-2.33	0.87	2111189048343657856	498.7	-0.87	0.19
4333627052547566464	638.3	-2.31	0.86	6076773820652573312	397.6	-0.86	0.36
6066743976821731200	354.2	-2.31	0.82	5779249135267388160	462.7	-0.82	0.26
4373808155229106048	415.7	-2.29	0.81	487598707882598912	333.9	-0.81	0.82
5814559886782561152	483.4	-2.28	0.81	2033040091219687424	495.0	-0.81	0.17
1562772473976590976	345.3	-2.27	0.78	2082877414211373056	514.7	-0.78	0.58
4167947800049312128	379.9	-2.27	0.75	4994896061572855680	242.8	-0.75	0.29
4382027799216609280	366.1	-2.26	0.73	5350758909803889152	584.9	-0.73	0.38

Table 6 (Continued)

Gaia DR3 ID	P_{LSP} (day)	$\Delta\phi_{ ext{RV}-G}$	$\mathrm{e}\Delta\phi$	Gaia DR3 ID	P_{LSP} (day)	$\Delta\phi_{ ext{RV}-G}$	$\mathrm{e}\Delta\phi$
5985892282645097728	335.5	-2.24	0.73	1384487655667958528	778.5	-0.73	0.57
5994696415836802304	687.5	-2.21	0.69	2038497375395267328	489.4	-0.69	0.28
5614629674553165568	594.9	-2.20	0.68	4755154010768073088	355.0	-0.68	0.62
2928002527094437504	678.3	-2.20	0.67	5357213966450101760	749.1	-0.67	0.29
5693199740370024576	363.9	-2.19	0.66	2004024043737361280	618.2	-0.66	1.03
6011162495794543104	304.5	-2.18	0.65	4660125660364324864	750.0	-0.65	0.23
5241758687171977216	704.5	-2.17	0.64	5717734865611449984	412.1	-0.64	1.16
6702743863564684800	393.9	-2.16	0.63	5730565341664785792	455.5	-0.63	0.31
2924804941112026240	525.0	-2.14	0.63	426958575728796032	536.2	-0.63	0.14
4487425953063740800	683.4	-2.10	0.38	5646561553800726784	265.4	-0.38	0.29
5914192369148073216	460.6	-2.09	0.33	4490750562689619584	273.9	-0.33	0.35
5846845430839141632	482.8	-2.07	0.29	4599913964043089408	380.3	-0.29	0.19
2192933679121399808	674.3	-2.02	0.17	5856898196963666816	692.4	-0.17	0.29
5970189980950373248	482.1	-2.02	0.15	2016488970841656320	510.8	-0.15	0.29

Table 7Gaia Phase Offsets, Continued

Gaia Phase Offsets, Continued							
Gaia DR3 ID	P_{LSP}	$\Delta \phi_{\mathrm{RV}-G}$	$e\Delta\phi$				
	(day)	7	,				
2021971062805508224	595.7	-0.09	0.30				
515032034094986112	663.0	-0.06	0.25				
2026398010175881856	490.4	0.29	0.61				
5243641635146938112	350.2	0.54	0.30				
6076305364288485888	310.9	0.57	0.05				
2231448029552393472	394.8	-4.85	0.15				
4688988660900813952	370.2	-4.83	0.58				
6641986087963535872	350.5	-3.71	0.27				
5348049300824404864	476.4	-3.58	0.44				
513141801805888896	712.0	-3.21	0.30				
2198382038425517696	720.6	-3.21	0.30				
5834193689811972480	466.2	-3.16	0.27				
1975711383110161664	464.2	-3.10	0.23				
5328193048536364672	384.6	-3.08	0.40				
6649474625438931840	289.4	-3.00	0.65				
2231049353507901568	547.2	-2.52	0.27				
5328530461163971968	514.8	-2.41	0.82				
5829828839147242240	435.6	-2.41	0.26				
1632704127922550272	447.1	-2.36	0.44				
2883038617538998144	518.9	-2.35	0.26				
5646198474439605760	539.1	-2.34	0.15				
6723996873576976768	324.7	-2.30	0.25				
1496998382733052928	321.9	-2.28	0.30				
6076713656747162624	623.0	-2.27	0.45				
2061975320222333696	544.2	-2.19	0.65				
5693299903313069312	318.1	-2.11	0.28				
4601169090926461184	384.2	-1.93	1.42				
2162696838801402624	507.8	-1.57	0.21				
5998083014713314944	398.2	-1.56	0.44				
385255959408720000	474.3	-1.31	0.33				
2030233136772978304	444.6	-1.14	0.55				
2895408329510160384	564.8	-1.09	0.73				
4617724574943762560	501.1	-1.01	1.05				
2045973161114595584	310.2	-0.96	0.24				
506098605197562624	570.6	-0.94	0.24				
6091162171552477440	406.6	-0.91	0.20				
4569516728144529664	406.0	-0.89	0.35				
4487550915135532288	411.8	-0.81	0.19				
4613334534251566848	534.7	-0.80	0.28				
513591398982018944	735.0	-0.75	0.30				

Table 7 (Continued)

Gaia DR3 ID	P _{LSP} (day)	$\Delta\phi_{\mathrm{RV}-G}$	$e\Delta\phi$
2014407045572567424	354.5	-0.68	0.46
186324619130226048	575.0	-0.67	1.66
505958902802490752	589.8	-0.67	0.60
5638830642723891328	655.7	-0.65	0.12

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